| 1 | ii iii | $\begin{aligned} & y^{\prime}=6 x^{2}-18 x+12 \\ & =12 \\ & y=7 \text { when } x=3 \end{aligned}$ <br> tgt is $y-7=12(x-3)$ verifying $(-1,-41)$ on tgt $y^{\prime}=0 \text { soi }$ <br> quadratic with 3 terms $x=1 \text { or } 2$ $y=3 \text { or } 2$ <br> cubic curve correct orientation touching $x$ - axis only at $(0.2,0)$ max and min correct $\qquad$ | M1 <br> M1 <br> B1 <br> M1 <br> A1 <br> M1 <br> M1 <br> A1 <br> A1 <br> G1 <br> G1 <br> G1 | condone one error subst of $x=3$ in their $y^{\prime}$ <br> f.t. their $y$ and $y^{\prime}$ or B2 for showing line joining $(3,7)$ and $(-1,-41)$ has gradient 12 <br> Their $y^{\prime}$ <br> Any valid attempt at solution or A1 for $(1,3)$ and A1 for $(2,2)$ marking to benefit of candidate <br> f.t. | 5 4 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |


| 2 | i | $\begin{aligned} & \hline y^{\prime}=3 x^{2}-6 x \\ & \text { use of } y^{\prime}=0 \\ & (0,1) \text { or }(2,-3) \end{aligned}$ <br> sign of $y^{\prime \prime}$ used to test or $y^{\prime}$ either side $\begin{aligned} & y^{\prime}(-1)=3+6=9 \\ & 3 x^{2}-6 x=9 \\ & x=3 \end{aligned}$ <br> At $\mathrm{P} y=1$ <br> grad normal $=-1 / 9$ cao $y-1=-1 / 9(x-3)$ <br> intercepts 12 and $4 / 3$ or use of $\begin{aligned} & \int_{0}^{12} 4 / 3-1 / 9 x \mathrm{~d} x \text { (their normal) } \\ & 1 / 2 \times 12 \times 4 / 3 \text { cao } \end{aligned}$ | B1 <br> M1 <br> A2 <br> T1 <br> B1 <br> M1 <br> A1 <br> B1 <br> B1 <br> M1 <br> B1 <br> A1 | condone one error <br> A1 for one correct or $x=0,2$ <br> SC B1 for $(0,1)$ from their $y^{\prime}$ <br> Dep't on M1 or $y$ either side or clear cubic sketch <br> ft for their $y^{\prime}$ <br> implies the M1 <br> ft their $(3,1)$ and their grad, not 9 ft their normal (linear) | 5 | 13 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| 3 | $x+x^{-1}$ soi | B1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $y^{\prime}=1-1 / x^{2}$ | B1 | $1-x^{-2}$ is acceptable |  |
| subs $x=1$ to get $y^{\prime}=0$ | B1 | Or solving $1-x^{-2}=0$ to obtain $x=1$ |  |  |
| M1ft | or checking $y^{\prime}$ before and after $x=1$ |  |  |  |
| $y^{\prime \prime}=2 x^{-3}$ attempted | A1 | Valid conclusion <br> First quadrant sketch scores B2 | 5 |  |


| Question |  | Answer | Marks | Guidance |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | (i) | $\begin{aligned} & x^{2}\left(9-x^{2}\right)=0 \text { soi } \\ & x=0 \text { and } \pm 3,[\text { so } a=3 \text { or } a=-3] \end{aligned}$ | B1 <br> B1 <br> [2] | $\begin{aligned} & 9 \times 0^{2}-0^{4}=0 \\ & 9 \times 3^{2}-3^{4}=0 \text { and } 9 \times(-3)^{2}-(-3)^{4}=0 \end{aligned}$ | B0 in each case if correct answer appears from clearly incorrect working $a= \pm 3$ without working does not score |
| 4 | (ii) | $\begin{aligned} & y^{\prime}=18 x-4 x^{3} \\ & y^{\prime \prime}=18-12 x^{2} \text { or } \mathrm{ft} \\ & \text { their } y^{\prime}=0 \text { soi } \\ & 2 x\left(9-2 x^{2}\right)=0 \text { so } x=0 \text { oe } \\ & x=0, y^{\prime \prime}=18 \text { cao so minimum } \\ & x= \pm \sqrt{4.5} \text { oe eg } \pm \frac{3 \sqrt{2}}{2} \end{aligned}$ | B1 <br> B1 <br> M1 <br> A1 <br> B1 <br> A1 <br> [6] | or $18 \times 0-4 \times 0^{3}=0$ oe or evaluation of $y^{\prime}$ at $\pm h$ oe where $h<\sqrt{4.5}$ <br> accept 2.12 or better for $\sqrt{4.5}$ |  |
| 4 | (iii) | $\int_{0}^{3}\left(9 x^{2}-x^{4}\right) \mathrm{d} x$ soi or ft $3 x^{3}-0.2 x^{5}$ <br> $\mathrm{F}[$ their positive $a$ ] [- $\mathrm{F}[0]]$ or (not and) F[0] - F[their negative $a$ ] $32.4 \text { oe cao }$ | M1 <br> A1 <br> M1 <br> A1 <br> [4] | condone omission of, or wrong limits <br> correct answer implies M1 dependent on at least one term correct | ignore + c <br> M0 if neither of the limits is 0 <br> M0 for $\mathrm{F}[0]$ - F[their positive $a$ ] <br> M0 for use of Trapezium Rule |


| $\mathbf{5}$ | B1 each term <br> their $\frac{d y}{d x}=0$ <br> correct step <br> $x=1 / 2$ c.a.o. | M1 <br> DM1 <br> A1 | s.o.i. | s.o.i. |
| :--- | :--- | :--- | :--- | :--- |


| $\mathbf{6}$ | $y^{\prime \prime}=2 x-6$ | B1 |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | $y^{\prime \prime}=0$ at $x=3$ | B1 |  |  |
|  | $y^{\prime}=0$ at $x=3$ |  |  |  |
| showing $y^{\prime}$ does not change sign | E1 | or that $y^{\prime \prime}$ changes sign | 4 |  |

